

Atty. Docket No.: LYRN002US0  
Customer ID No. 58,293

Please amend the claims as follows:

1-31. (Cancelled)

32. (Cancelled) A method of encrypting data, comprising:

choosing a modulus C for modular calculations, wherein C is a w-bit number, and wherein the modulus C is selected from the group consisting of (a) w-big and w-heavy, and (b) w-little and w-light; and

using the modulus to encrypt data.

33. (Cancelled) The method of claim 32, further comprising:

performing a ring arithmetic function on numbers, including (a) using a residue number multiplication process, (b) converting to a first basis using a mixed radix system, and (c) converting to a second basis using a mixed radix system.

34. (Cancelled) The method of claim 32, wherein the modulus C is of the form  $2^w - L$ , and wherein L is a low Hamming weight odd integer less than  $2^{(w-1)/2}$ .

35. (Cancelled) The method of claim 34, further comprising:

calculating the modulus C by a process including

(a) splitting a number  $P < 2^{2w}$  into 2 w-bit words  $H_1$  and  $L_1$ ;

(b) calculating  $S_1 = L_1 + (H_1 2^{x_1}) + (H_1 2^{x_2}) + \dots + (H_1 2^{x_k}) + H_1$ , wherein  $(w-3)/2 > x_1 > x_2 > \dots > x_k > 0$  and  $k \ll w$ ;

(c) splitting  $S_1$  into two w-bit words  $H_2$  and  $L_2$ ;

(d) computing  $S_2 = L_2 + (H_2 2^{x_1}) + (H_2 2^{x_2}) + \dots + (H_2 2^{x_k}) + H_2$ ;

(e) computing  $S_3 = S_2 + (2^{x_1} + \dots + 2^{x_k} + 1)$ ;

(f) determining the modulus C by comparing  $S_3$  to  $2^w$ , wherein the modulus  $C = S_2$  if  $S_3 < 2^w$ , and wherein the modulus  $C = S_3 - 2^w$  if  $S_3 \geq 2^w$ ;  
wherein the modulus C is a residue.

Atty. Docket No.: LYRN002US0  
Customer ID No. 58,293

36. (Cancelled) The method of claim 32, wherein the modulus  $C$  is of the form  $2^w + L$ , and wherein the modulus  $C$  has a Hamming weight close to 1.

37. (Cancelled) The method of Claim 32, wherein the method of encrypting data comprises a method of cryptographic hashing.

38. (Cancelled) The method of Claim 32, wherein the modulus  $C$  is  $w$ -big and  $w$ -heavy.

39. (Cancelled) The method of Claim 32, wherein the modulus  $C$  is  $w$ -little and  $w$ -light.

40.(Cancelled) A method of encrypting data, comprising:

receiving data; and

using a modulus  $C$  to encrypt the data, wherein  $C$  is a  $w$ -bit number, wherein the modulus  $C$  is of the form  $2^w - x$ , wherein  $x = \pm L$ , wherein  $L$  is a low Hamming weight odd integer less than  $2^{(w-1)/2}$ , and wherein the modulus  $C$  is selected from the group consisting of (a)  $w$ -big and  $w$ -heavy, and (b)  $w$ -little and  $w$ -light; and

outputting the encrypted data.

41.(Cancelled) The method of claim 40, wherein the modulus  $C$  is  $w$ -big.

42.(Cancelled) The method of claim 40, wherein the modulus  $C$  is  $w$ -heavy.

43.(Cancelled) The method of claim 40, wherein the modulus  $C$  is  $w$ -little.

44.(Cancelled) The method of claim 40, wherein the modulus  $C$  is  $w$ -light.

45.(Cancelled) The method of claim 40, wherein  $x = L$ .

46.(Cancelled) The method of claim 40, wherein  $x = -L$ .

Atty. Docket No.: LYRN002US0  
Customer ID No. 58,293

47. (Cancelled) The method of claim 40, wherein the step of encrypting the data includes the step of performing a ring arithmetic function on numbers, including (a) using a residue number multiplication process, (b) converting to a first basis using a mixed radix system, and (c) converting to a second basis using a mixed radix system.

48. (Cancelled) The method of claim 40, further comprising:

calculating the modulus C by a process including

- (a) providing a number  $P < 2^{2w}$ ;
- (b) splitting P into 2 w-bit words  $H_1$  and  $L_1$ ;
- (c) calculating  $S_1 = L_1 + (H_1 2^{x_1}) + (H_1 2^{x_2}) + \dots + (H_1 2^{x_k}) + H_1$ , wherein  $(w-3)/2 > x_1 > x_2 > \dots > x_k > 0$  and  $k \ll w$ ;
- (d) splitting  $S_1$  into two w-bit words  $H_2$  and  $L_2$ ;
- (e) computing  $S_2 = L_2 + (H_2 2^{x_1}) + (H_2 2^{x_2}) + \dots + (H_2 2^{x_k}) + H_2$ ;
- (f) computing  $S_3 = S_2 + (2^{x_1} + \dots + 2^{x_k} + 1)$ ;
- (g) determining the modulus C by comparing  $S_3$  to  $2^w$ , wherein the modulus C is a residue, wherein the modulus  $C = S_2$  if  $S_3 < 2^w$ , and wherein the modulus  $C = S_3 - 2^w$  if  $S_3 \geq 2^w$ .

49. (Cancelled) The method of claim 40, wherein the modulus C has a Hamming weight close to 1.

50. (Cancelled) The method of Claim 40, wherein the method of encrypting data comprises a method of cryptographic hashing.

51. (Cancelled) The method of claim 32, wherein  $C = 2^w - 2^{x_1} - 2^{x_2} - \dots - 2^{x_k} - 1$ , wherein  $(w-3)/2 > x_1 > x_2 > \dots > x_k > 0$ , and wherein  $k \gg w$ .

Atty. Docket No.: LYRN002US0  
Customer ID No. 58,293

52. (Cancelled) The method of claim 32, further comprising:

choosing a first basis  $(m_1, m_2, \dots, m_t)$  and a second basis  $(m_{t+1}, m_{t+2}, \dots, m_{2t})$ , wherein  $m_1, \dots, m_{2t}$  are moduli;

calculating a product  $M = m_1 m_2 \dots m_t$ ;

calculating a product  $W = m_{t+1} m_{t+2} \dots m_{2t}$ ; and

calculating a product  $ABM^{-1} \bmod p$  for  $n$ -bit numbers  $A$  and  $B$  by (a) computing  $Q \bmod M$  in the first basis such that  $AB + Qp = RM$  for some integral value  $R$  and for a number  $p$  which is prime relative to  $M$  and  $W$ ; (b) converting  $Q$  to the second basis,  $Q \bmod W$ ; and (c) computing  $R$  in the second basis,  $R \bmod W$ , wherein  $R = (AB + Qp) M^{-1} \bmod W$  and  $R \bmod p = ABM^{-1} \bmod p$ .

53. (Cancelled) The method of claim 52 wherein, for  $i = 1$  to  $2t$ ,  $2^{k-1} \leq m_i \leq 2^k$ , and wherein  $m_1, \dots, m_{2t}$  are pairwise mutually prime.

54. (Cancelled) The method of claim 53, wherein  $t \geq (n+1)/k$ , where  $n$  is the bit length of the numbers being multiplied.

55. (Cancelled) The method of claim 54, wherein  $p$  is an  $n$ -bit number, and wherein  $p$  is a prime number.

56. (Cancelled) The method of claim 52, further comprising converting  $R$  to the first basis,  $R \bmod M$ .

57. (Cancelled) The method of claim 52, wherein the step of calculating a product  $ABM^{-1} \bmod p$  is performed iteratively and includes at least first and second subsequent iterations, and wherein the value of  $R$  calculated in the first iteration is utilized as the input value of  $R$  in the second iteration.

58. (Cancelled) The method of claim 52, wherein the data is encrypted using asymmetric encryption.

Atty. Docket No.: LYRN002US0  
Customer ID No. 58,293

59. (Cancelled) The method of claim 52, wherein the data is encrypted using symmetric encryption.

60. (New) A method of encrypting data, comprising:

choosing a modulus  $C$  for modular calculations, wherein  $C$  is a  $w$ -bit number, and wherein the modulus  $C$  is selected from the group consisting of (a)  $w$ -big and  $w$ -heavy, and (b)  $w$ -little and  $w$ -light; and

using the modulus to encrypt data;

wherein  $C = 2^w - 2^{x_1} - 2^{x_2} - \dots - 2^{x_k} - 1$ , wherein  $(w - 3)/2 > x_1 > x_2 > \dots > x_k > 0$ , and wherein  $k \gg w$ .

61. (New) The method of claim 60, further comprising:

performing a ring arithmetic function on numbers, including (a) using a residue number multiplication process, (b) converting to a first basis using a mixed radix system, and (c) converting to a second basis using a mixed radix system.

62. (New) The method of claim 60, wherein the modulus  $C$  is of the form  $2^w - L$ , and wherein  $L$  is a low Hamming weight odd integer less than  $2^{(w-1)/2}$ .

63. (New) The method of claim 62, further comprising:

calculating the modulus  $C$  by a process including

(a) splitting a number  $P < 2^{2w}$  into 2  $w$ -bit words  $H_1$  and  $L_1$ ;

(b) calculating  $S_1 = L_1 + (H_1 2^{x_1}) + (H_1 2^{x_2}) + \dots + (H_1 2^{x_k}) + H_1$ , wherein  $(w-3)/2 > x_1 > x_2 > \dots > x_k > 0$  and  $k \ll w$ ;

(c) splitting  $S_1$  into two  $w$ -bit words  $H_2$  and  $L_2$ ;

(d) computing  $S_2 = L_2 + (H_2 2^{x_1}) + (H_2 2^{x_2}) + \dots + (H_2 2^{x_k}) + H_2$ ;

(e) computing  $S_3 = S_2 + (2^{x_1} + \dots + 2^{x_k} + 1)$ ;

(f) determining the modulus  $C$  by comparing  $S_3$  to  $2w$ , wherein the modulus  $C = S_2$  if  $S_3 < 2^w$ , and wherein the modulus  $C = S_3 - 2^w$  if  $S_3 \geq 2^w$ ;  
wherein the modulus  $C$  is a residue.

Atty. Docket No.: LYRN002US0  
Customer ID No. 58,293

64. (New) The method of claim 60, wherein the modulus  $C$  is of the form  $2^w + L$ , and wherein the modulus  $C$  has a Hamming weight close to 1.

65. (New) The method of Claim 60, wherein the method of encrypting data comprises a method of cryptographic hashing.

66. (New) The method of Claim 60, wherein the modulus  $C$  is  $w$ -big and  $w$ -heavy.

67. (New) The method of Claim 60, wherein the modulus  $C$  is  $w$ -little and  $w$ -light.

68. (New) A method of encrypting data, comprising:

receiving data; and

using a modulus  $C$  to encrypt the data, wherein  $C$  is a  $w$ -bit number, wherein the modulus  $C$  is of the form  $2^w - x$ , wherein  $x = \pm L$ , wherein  $L$  is a low Hamming weight odd integer less than  $2^{(w-1)/2}$ , and wherein the modulus  $C$  is selected from the group consisting of (a)  $w$ -big and  $w$ -heavy, and (b)  $w$ -little and  $w$ -light; and

outputting the encrypted data;

wherein the modulus  $C$  is calculated by a process including

(a) providing a number  $P < 2^{2w}$ ;

(b) splitting  $P$  into 2  $w$ -bit words  $H_1$  and  $L_1$ ;

(c) calculating  $S_1 = L_1 + (H_1 2^{x_1}) + (H_1 2^{x_2}) + \dots + (H_1 2^{x_k}) + H_1$ , wherein  $(w-3)/2 > x_1 > x_2 > \dots > x_k > 0$  and  $k \ll w$ ;

(d) splitting  $S_1$  into two  $w$ -bit words  $H_2$  and  $L_2$ ;

(e) computing  $S_2 = L_2 + (H_2 2^{x_1}) + (H_2 2^{x_2}) + \dots + (H_2 2^{x_k}) + H_2$ ;

(f) computing  $S_3 = S_2 + (2^{x_1} + \dots + 2^{x_k} + 1)$ ; and

(g) determining the modulus  $C$  by comparing  $S_3$  to  $2^w$ , wherein the modulus  $C$  is a residue, wherein the modulus  $C = S_2$  if  $S_3 < 2^w$ , and wherein the modulus  $C = S_3 - 2^w$  if  $S_3 \geq 2^w$ .

69. (New) The method of claim 68, wherein the modulus  $C$  is  $w$ -big.

Atty. Docket No.: LYRN002US0  
Customer ID No. 58,293

70.(New) The method of claim 68, wherein the modulus C is w-heavy.

71.(New) The method of claim 68, wherein the modulus C is w-little.

72.(New) The method of claim 68, wherein the modulus C is w-light.

73.(New) The method of claim 68, wherein  $x = L$ .

74.(New) The method of claim 68, wherein  $x = -L$ .

75. (New) The method of claim 68, wherein the step of encrypting the data includes the step of performing a ring arithmetic function on numbers, including (a) using a residue number multiplication process, (b) converting to a first basis using a mixed radix system, and (c) converting to a second basis using a mixed radix system.

76. (New) The method of claim 68, wherein the modulus C has a Hamming weight close to 1.

77. (New) The method of Claim 68, wherein the method of encrypting data comprises a method of cryptographic hashing.

78. (New) A method for encrypting data, comprising:

choosing a first basis  $(m_1, m_2, \dots, m_t)$  and a second basis  $(m_{t+1}, m_{t+2}, \dots, m_{2t})$ , wherein  $m_1, \dots, m_{2t}$  are moduli and wherein, for any  $m_i \in (m_1, m_2, \dots, m_{2t})$ ,  $m_i$  is a w-bit number selected from the group consisting of (a) w-big and w-heavy, and (b) w-little and w-light; and

encrypting data by performing a ring arithmetic function on numbers by (a) using a residue number multiplication process, (b) converting to the first basis using a mixed radix system, and (c) converting to the second basis using a mixed radix system;

wherein the residue number multiplication process includes

(a) calculating a product  $M = m_1 m_2 \dots m_t$ .

Atty. Docket No.: LYRN002US0  
Customer ID No. 58,293

- (b) calculating a product  $W = m_{t+1}m_{t+2} \dots m_{2t}$ , and
- (c) calculating a product  $ABM^{-1} \bmod p$  for n-bit numbers A and B by
  - (i) computing  $Q \bmod M$  in the first basis such that  $AB + Qp = RM$  for some integral value R and for a number p which is prime relative to M and W;
  - (ii) converting Q to the second basis,  $Q \bmod W$ , and
  - (iii) computing R in the second basis,  $R \bmod W$ , wherein  $R = (AB + Qp) M^{-1} \bmod W$  and  $R \bmod p = ABM^{-1} \bmod p$ .

79. (New) The method of claim 78 wherein, for  $i = 1$  to  $2t$ ,  $2^{k-1} \leq m_i \leq 2^k$ , and wherein  $m_1, \dots, m_{2t}$  are pairwise mutually prime.

80. (New) The method of claim 79, wherein  $t \geq (n+1)/k$ , where n is the bit length of the numbers being multiplied.

81. (New) The method of claim 80, wherein p is an n-bit number, and wherein p is a prime number.

82. (New) The method of claim 78, further comprising converting R to the first basis,  $R \bmod M$ .

83. (New) The method of claim 78, wherein the step of calculating a product  $ABM^{-1} \bmod p$  is performed iteratively and includes at least first and second subsequent iterations, and wherein the value of R calculated in the first iteration is utilized as the input value of R in the second iteration.

84. (New) The method of claim 78, wherein the data is encrypted using asymmetric encryption.

85. (New) The method of claim 78, wherein the data is encrypted using symmetric encryption.

86. (New) The method of claim 78, wherein  $m_i$  is of the form  $2^w + L$ , and wherein  $m_i$  has a Hamming weight close to 1.



Atty. Docket No.: LYRN002US0  
Customer ID No. 58,293

87. (New) The method of Claim 78, wherein  $m_i$  is either w-big and w-heavy, or w-little and w-light.